

1. A method of identifying a user, comprising the steps of:

a) selecting a modulus p from the group of equations consisting of:

$$p=(2^{dk}-2^{ck}-1)/r,$$

where $0<2c\leq d$, where $r \neq 1$, and where $GCD(c,d)=1$;

$$p=(2^{dk}-2^{(d-1)k}+2^{(d-2)k}-\dots-2^k+1)/r,$$

where d is even, and where k is not equal to 2 (mod 4);

$$p=(2^{dk}-2^{ck}-1)/r,$$

where $3d<6c<4d$, and where $GCD(c,d)=1$;

$$p=(2^{dk}-2^{ck}+1)/r,$$

where $0<2c\leq d$, where $r \neq 1$, and where $GCD(c,d)=1$; and

$$p=(2^{4k}-2^{3k}+2^{2k}+1)/r;$$

b) selecting an elliptic curve E and an order q ;

c) selecting a basepoint G ;

- d) generating a private key w ;
- e) generating a public key $W=wG$;
- f) distributing p , E , q , G , and W in an authentic manner;
- g) retrieving, by a prover, the prover's private key w ;
- h) retrieving, by a verifier, the prover's public key W ;
- i) generating, by the prover, a private integer k ;
- j) combining, by the prover, k and the prover's G to form K using the form of the prover's

modulus p ;

- k) sending, by the prover, K to the verifier;
- l) sending, by the verifier, a challenge integer c to prover;
- m) combining, by the prover, c , k , and w to form a response integer v ;
- n) sending, by the prover, v to the verifier; and
- o) combining, by the verifier, cG , K , and W using the form of the prover's modulus p and checking to see if the combination is equal to vG , if so the user is identified as the user, otherwise the user is not identified as the user.

2. A method of generating a digital signature, comprising the steps of:

- a) selecting a modulus p from the group of equations consisting of:

$$p=(2^{dk}-2^{ck}-1)/r,$$

where $0 < 2c \leq d$, where $r \neq 1$, and where $GCD(c, d) = 1$;

$$p=(2^{dk}-2^{(d-1)k}+2^{(d-2)k}-\dots-2^k+1)/r,$$

where d is even, and where k is not equal to 2 (mod 4);

$$p=(2^{dk}-2^{ck}-1)/r,$$

where $3d < 6c < 4d$, and where $GCD(c, d)=1$;

$$p=(2^{dk}-2^{ck}+1)/r,$$

where $0 < 2c \leq d$, where $r \neq 1$, and where $GCD(c, d)=1$; and

$$p=(2^{4k}-2^{3k}+2^{2k}+1)/r;$$

- b) selecting an elliptic curve E and an order q ;
- c) selecting a basepoint G ;
- d) generating a private key w ;
- e) generating a public key $W=wG$;
- f) distributing p , E , q , G , and W in an authentic manner;
- g) retrieving, by a signer, the signer's private key w ;
- h) generating, by the signer, a private integer k ;
- i) combining, by the signer, k and G to form K using the form of the prover's modulus p ;
- j) combining, by the signer, K and a message M to form an integer h ;

- k) combining by the signer, h , k , and w to form an integer s ; and
- l) sending, by the signer, M and (K,s) as a digital signature of M .

3. The method of claim 1, further including the steps of:

- a) retrieving, by the verifier, the prover's public key W ;
- b) receiving, by the verifier, M and (K,s) ;
- c) combining, by the verifier, K and M to form an integer h ; and
- d) combining, by the verifier, h , k , and W using the form of the prover's modulus p and

checking to see if the combination is equal to sG , if so then the digital signature is verified, otherwise the digital signature is not verified.

4. A method of generating a digital signature, comprising the steps of:

- a) selecting a modulus p from the group of equations consisting of:

$$p=(2^{dk}-2^{ck}-1)/r,$$

where $0 < 2c \leq d$, where $r \neq 1$, and where $GCD(c,d)=1$;

$$p=(2^{dk}-2^{(d-1)k}+2^{(d-2)k}-\dots-2^k+1)/r,$$

where d is even, and where k is not equal to 2 (mod 4);

$$p=(2^{dk}-2^{ck}-1)/r,$$

where $3d < 6c < 4d$, and where $GCD(c, d) = 1$;

$$p = (2^{dk} - 2^{ck} + 1) / r,$$

where $0 < 2c \leq d$, where $r \neq 1$, and where $GCD(c, d) = 1$; and

$$p = (2^{4k} - 2^{3k} + 2^{2k} + 1) / r;$$

- b) selecting an elliptic curve E and an order q ;
- c) selecting a basepoint G ;
- d) generating a private key w ;
- e) generating a public key $W = wG$;
- f) distributing p , E , q , G , and W in an authentic manner;
- g) retrieving, by a signer, the signer's private key w ;
- h) generating, by the signer, a private integer k ;
- i) combining, by the signer, k and G to form K using the form of the prover's modulus p ;
- j) combining, by the signer, K and a message M to form an integer h ;
- k) combining by the signer, h , k , and w to form an integer s ; and
- l) sending, by the signer, M and (h, s) as a digital signature of M .

5. The method of claim 4, further including the steps of:

- a) retrieving, by the verifier, the prover's public key W ;

- b) receiving, by the verifier, M and (h,s) ;
- c) combining, by the verifier, h , W , and sG using the form of the prover's modulus p to form K ;
- d) combining, by the verifier, K and M to form an integer h' ; and
- e) checking, by the verifier, that h is equal to h' , if so then the digital signature is verified, otherwise the digital signature is not verified.